

# **LECTURE 18: STEREOSCOPIC PARTICLE IMAGE VELOCIMETRY - PART 02**

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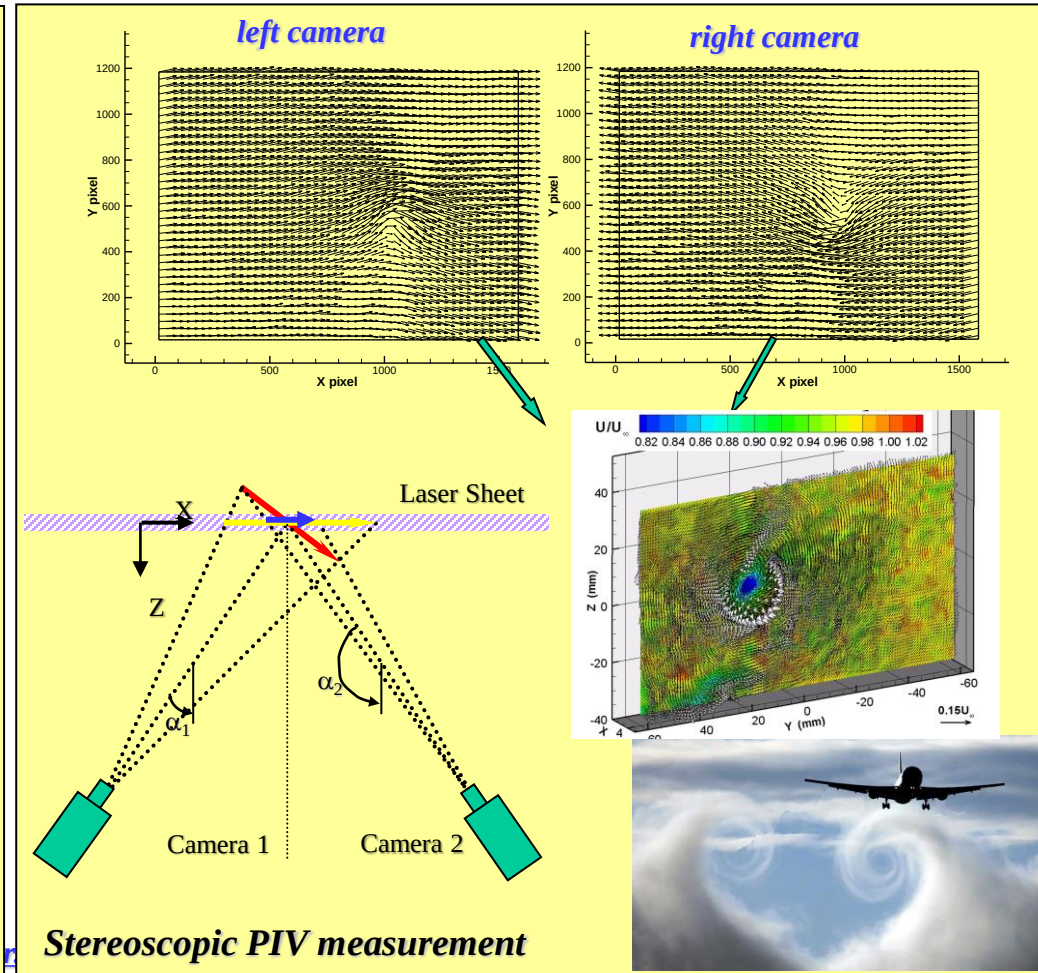
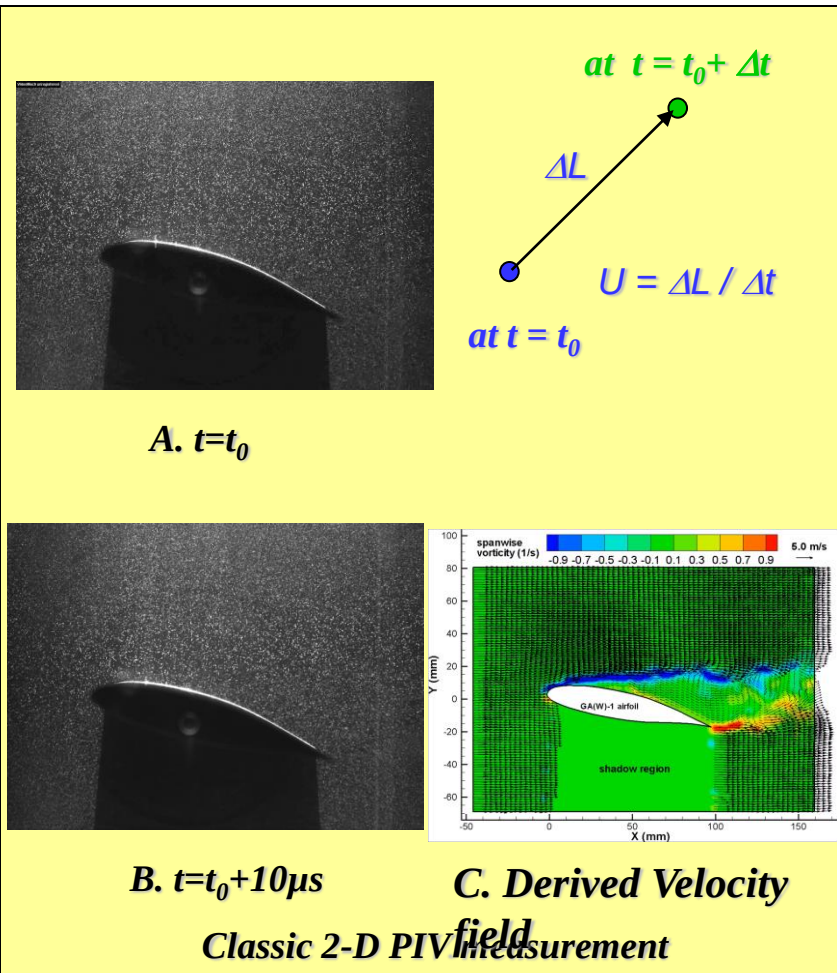
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# □ PARTICLE-BASED TECHNIQUES: PARTICLE IMAGE VELOCIMETRY (PIV)

- To *seed fluid flows* with small tracer *particles* ( $\sim \mu\text{m}$ ), and assume the tracer particles moving with the same velocity as the low fluid flows.
- To measure the *displacements* ( $\Delta L$ ) of the tracer particles between *known time interval* ( $\Delta t$ ). The local velocity of fluid flow is calculated by  $U = \Delta L / \Delta t$ .



# Dual-plane Stereoscopic PIV System!? Why???

- **Vorticity vector is defined as the curl of the velocity vector :**

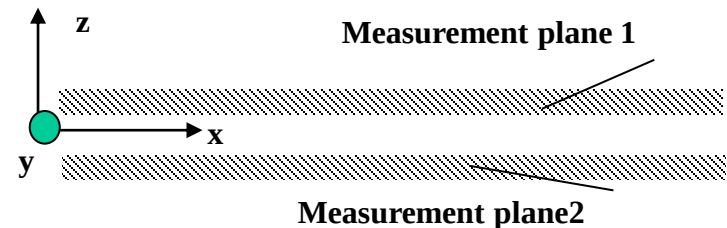
$$\varpi_z = \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y};$$

$$\varpi_x = \frac{\partial w}{\partial y} - \frac{\partial v}{\partial z}; \quad \varpi_y = \frac{\partial u}{\partial z} - \frac{\partial w}{\partial x}$$

- **Simultaneous measurements of velocity vectors (three-components) at least at two spatially separated planes are need in order to get all three-components of vorticity vectors.**
- **Development of a Dual-plane Stereoscopic PIV system to achieve the stereoscopic PIV measurements at two parallel planes simultaneously.**



“Classical” PIV or SPIV systems can only provide measurement results in one single plane instantaneously

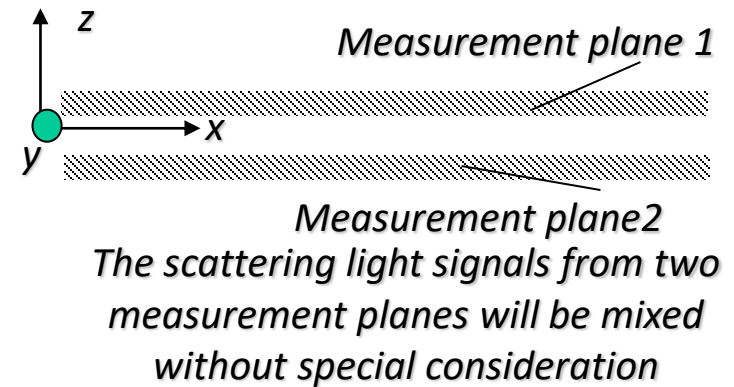


Dual-plane Stereoscopic PIV system can achieve stereoscopic PIV measurements at two parallel planes simultaneously

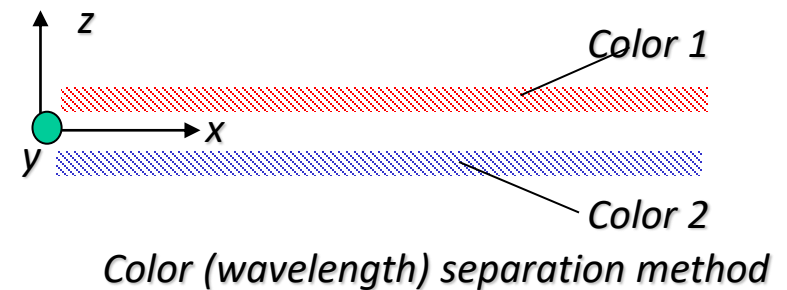
- [Hu H, Saga T, Kobayashi T, Taniguchi N, Yashuki M, "Dual-plane Stereoscopic Particle Image Velocimetry: System Setup and Its Application on a Lobed Jet Mixing Flow" Experiments in Fluids, Vol. 31, No. 3, pp277-293, 2001](#)

# Dual-plane Stereoscopic PIV System!? How???

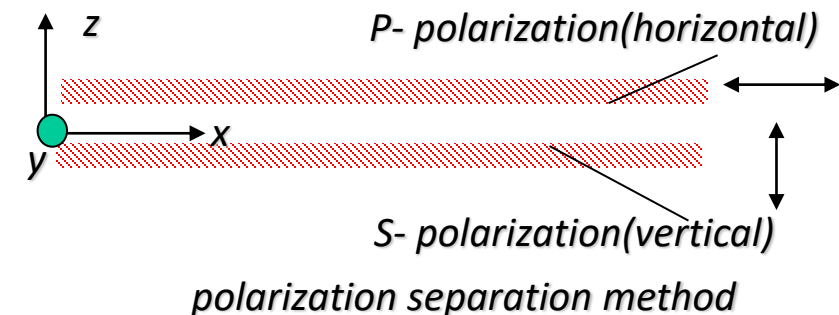
- Key point for the simultaneous stereoscopic PIV measurements at two parallel planes is to achieve *scattering light separation*.



- *Color (wavelength) separation method*.



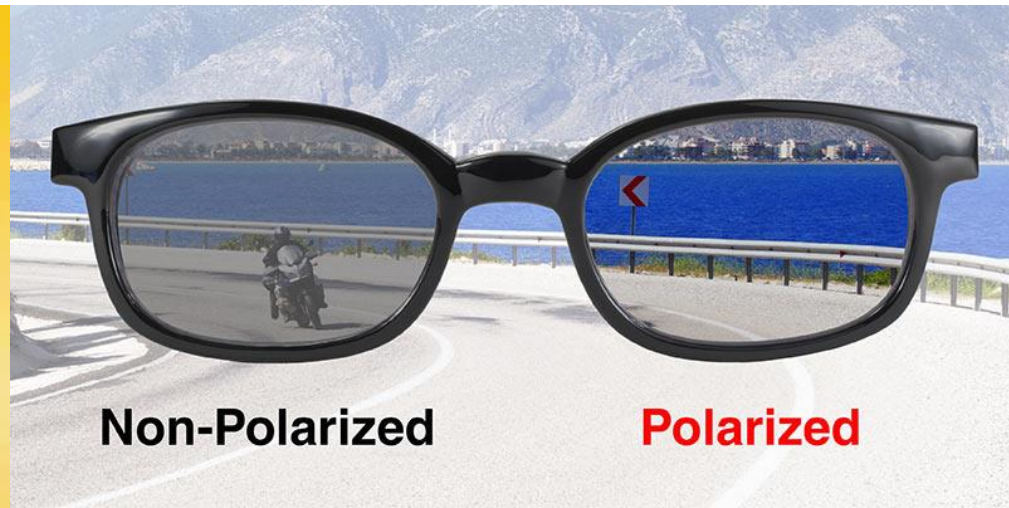
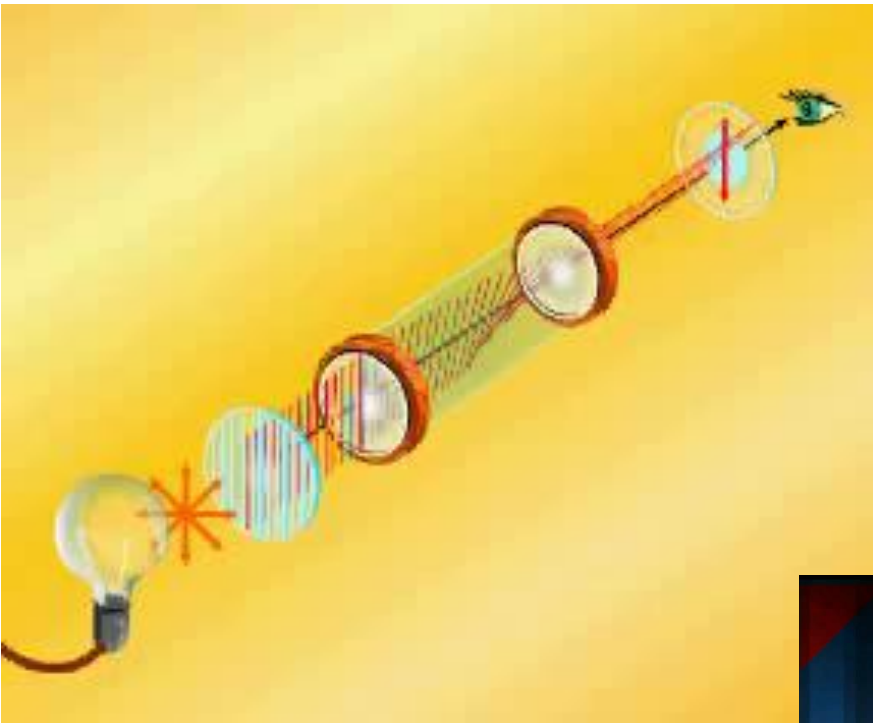
- *Polarization separation method*.
- The polarization of Mie scattering light is conservative in air.



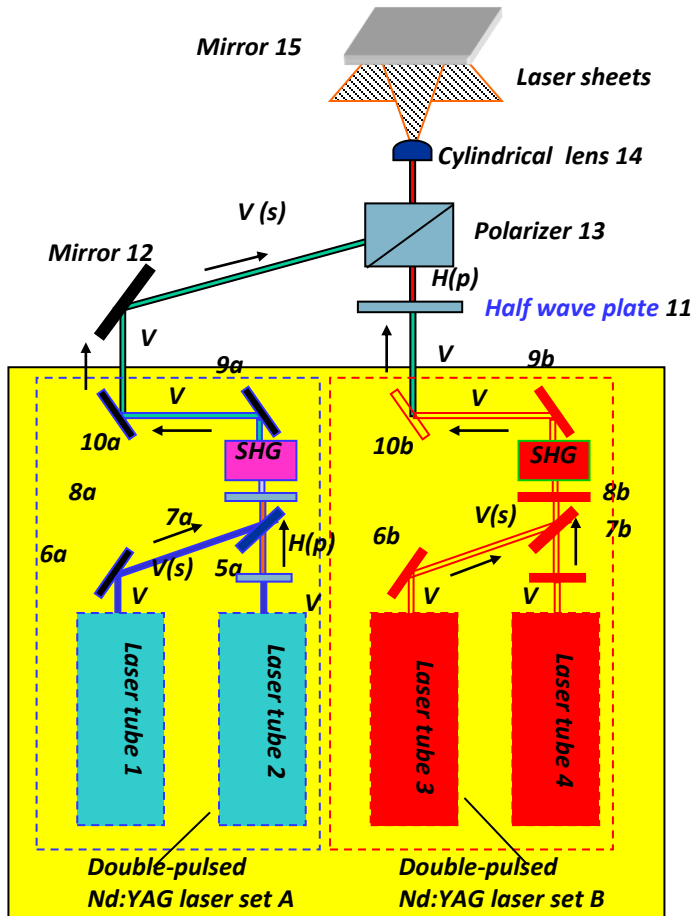
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# Polarization of light



# Optical Set-up for Dual-plane SPIV Illumination

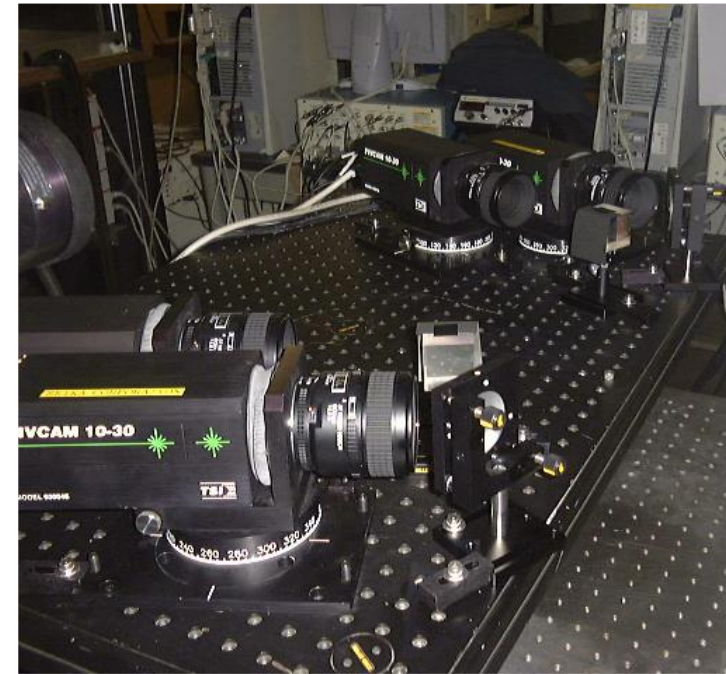
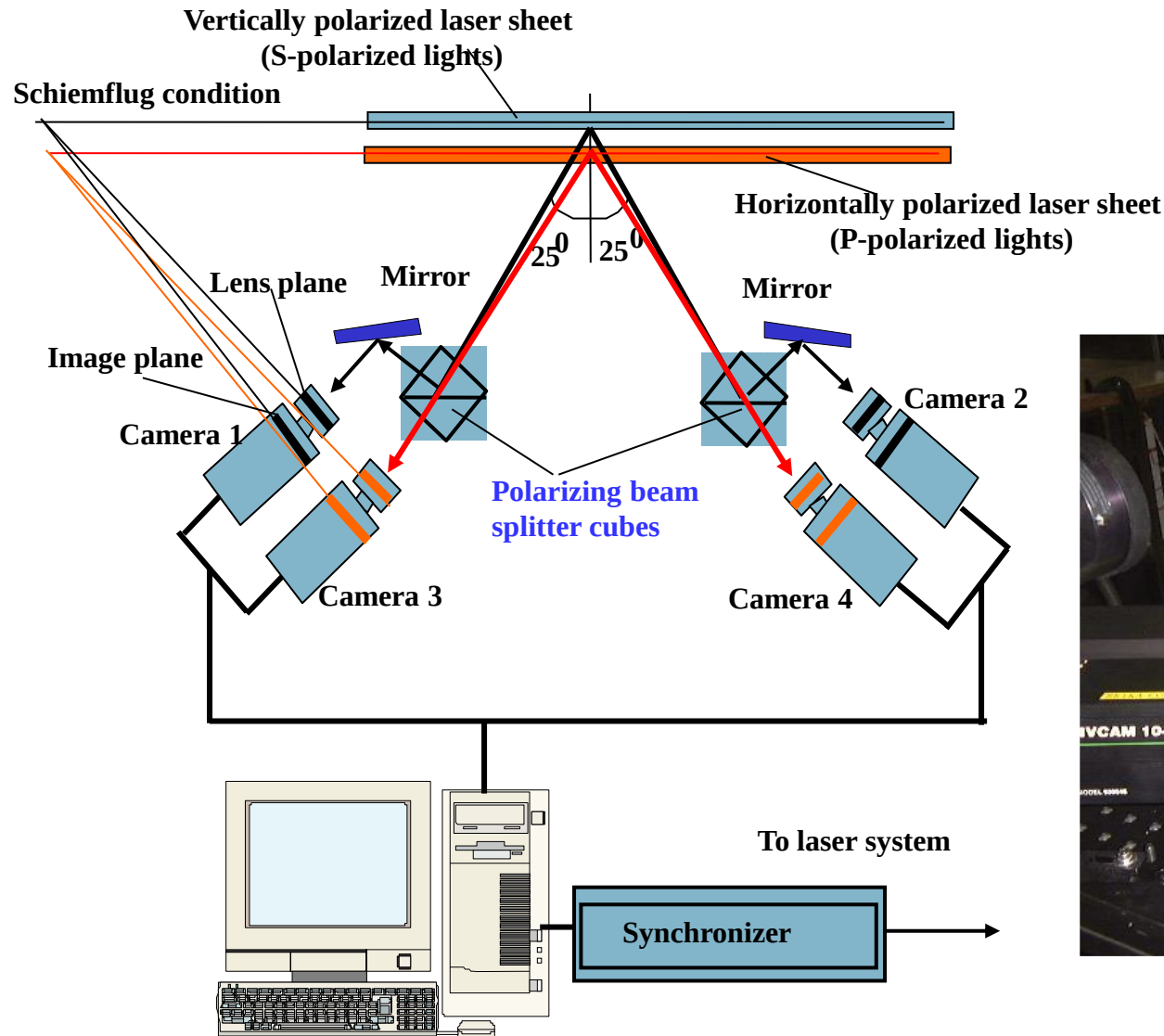


1 to 4 : laser tube  
6,9, 10,15: mirror  
14: cylinder lens

5,8,11: half wave plate  
7,13: polarizer

- [Hu H, Saga T, Kobayashi T, Taniguchi N, Yashuki M](#), "Dual-plane Stereoscopic Particle Image Velocimetry: System Setup and Its Application on a Lobed Jet Mixing Flow" *Experiments in Fluids*, Vol. 31, No. 3, pp277-293, 2001

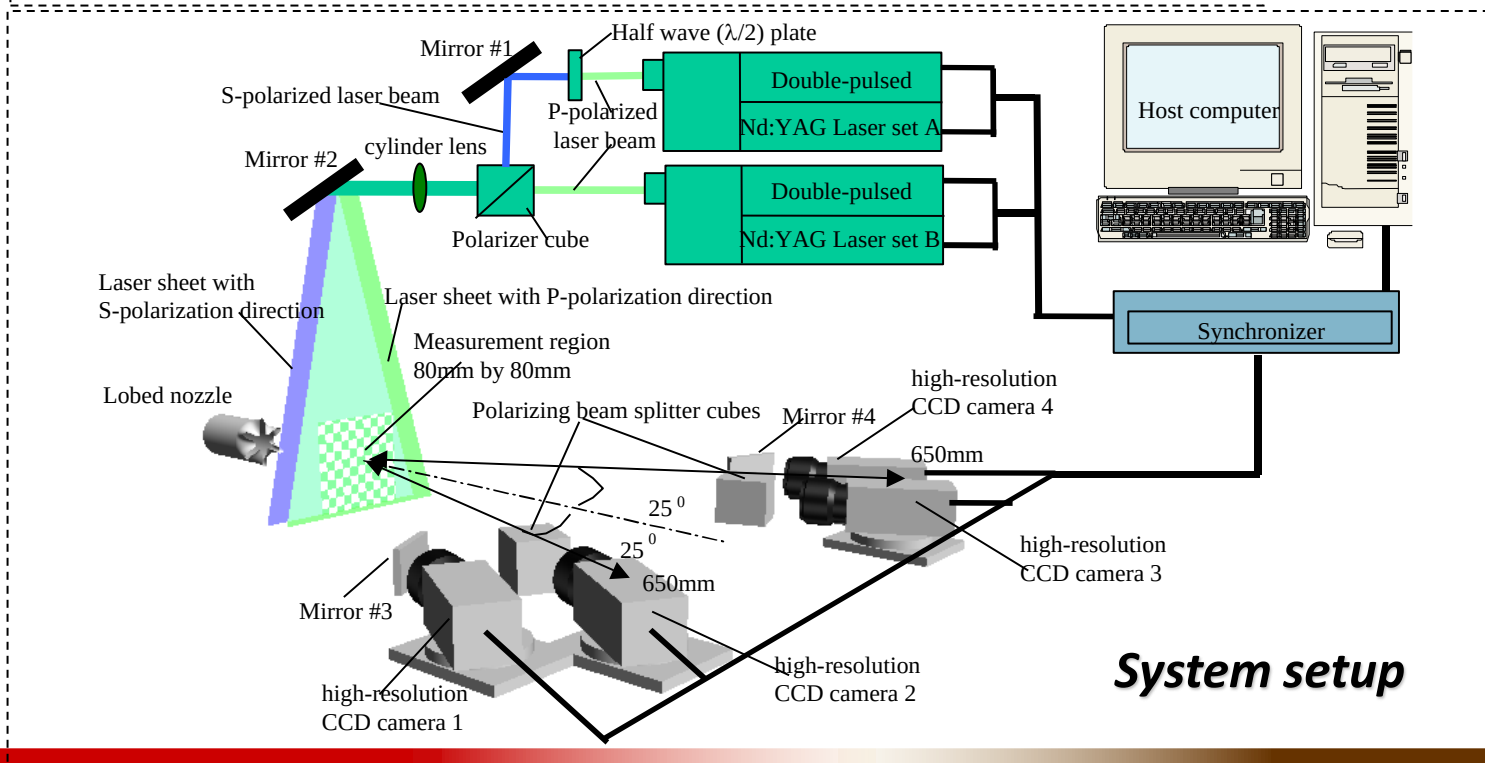
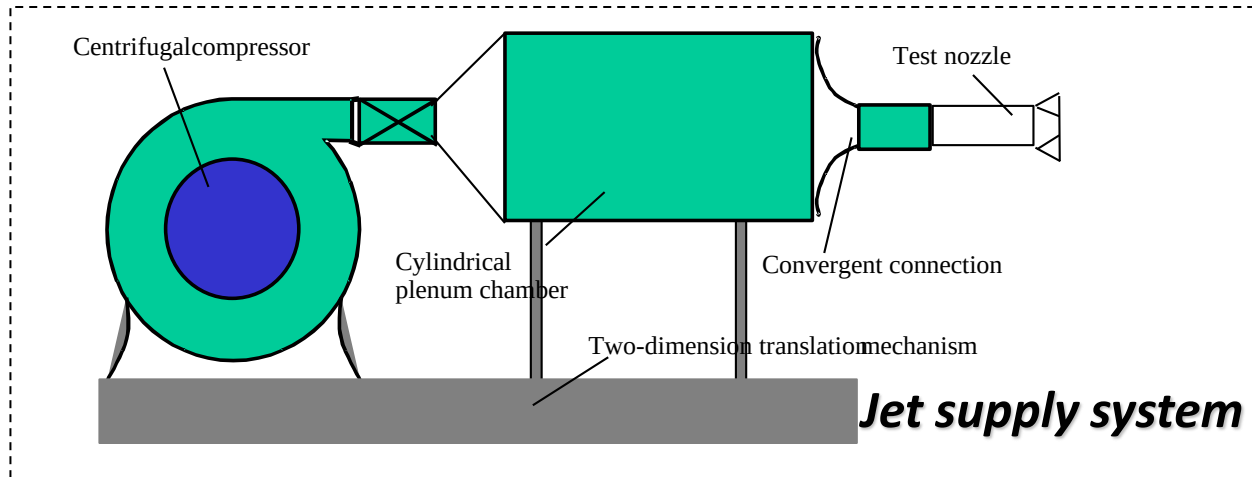
# Set-up for Dual-plane SPIV Image Recording



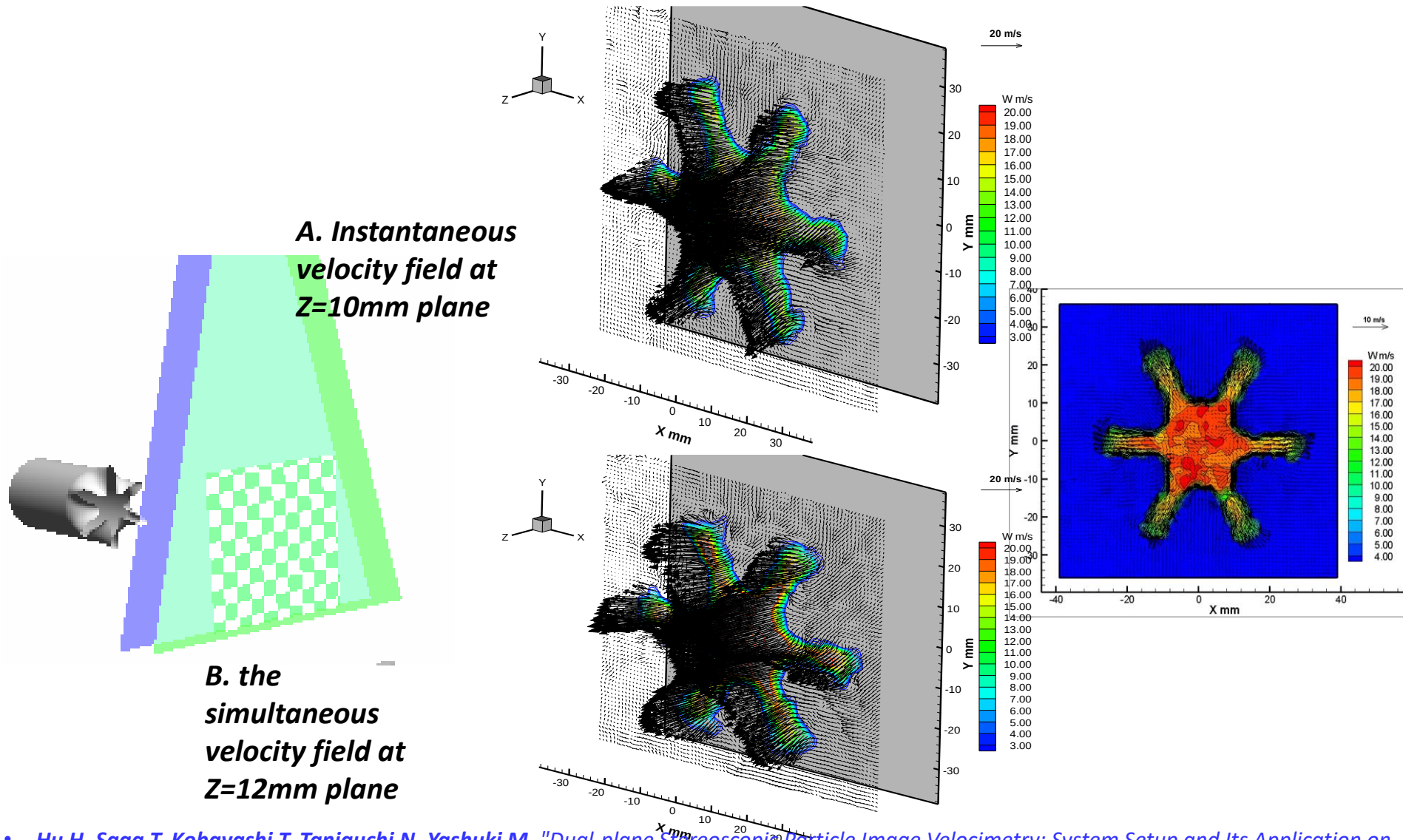
- [Hu H, Saga T, Kobayashi T, Taniguchi N, Yashuki M](#), "Dual-plane Stereoscopic Particle Image Velocimetry: System Setup and Its Application on a Lobed Jet Mixing Flow" *Experiments in Fluids*, Vol. 31, No. 3, pp277-293, 2001



# Experimental Set-up



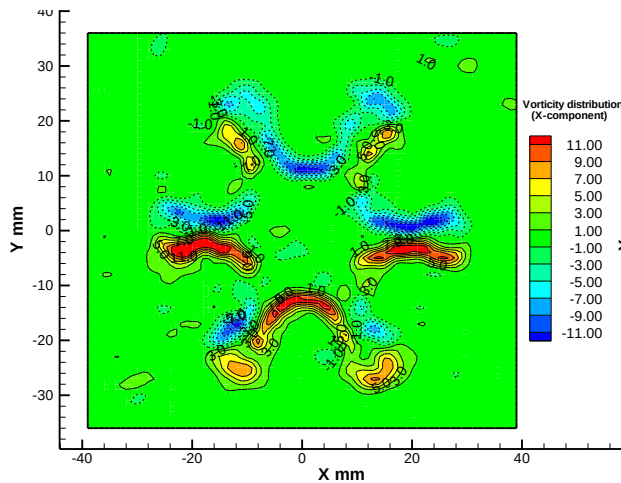
# The Simultaneous Measurement Results of the Dual-plane Stereoscopic PIV System at Two Parallel Planes



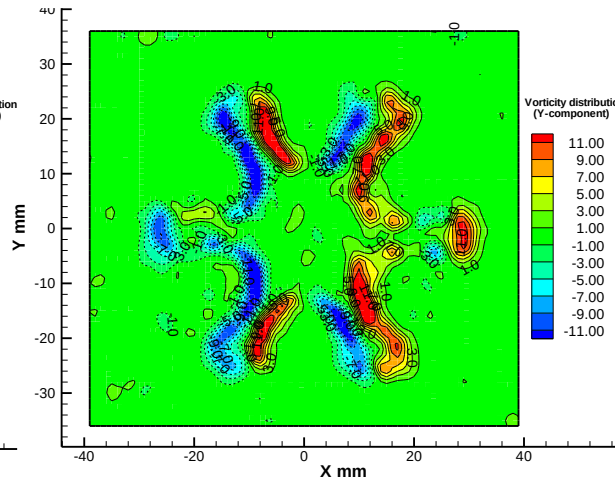
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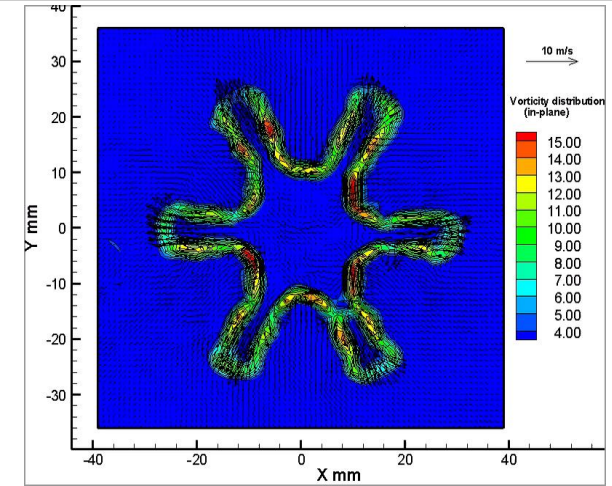
# Distributions of Three Components of Vorticity Vectors



a. instantaneous vorticity  $\varpi_x$

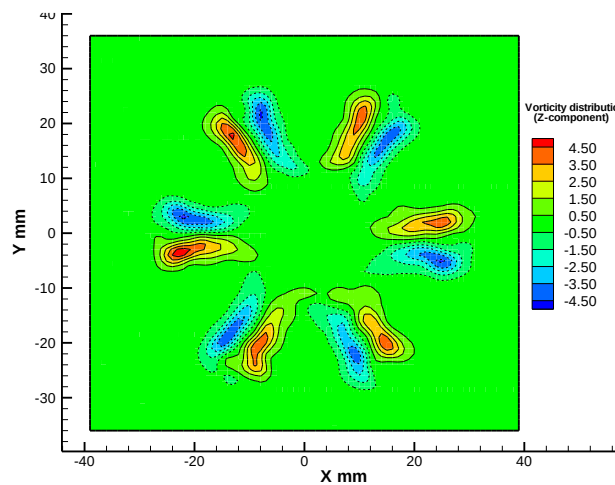
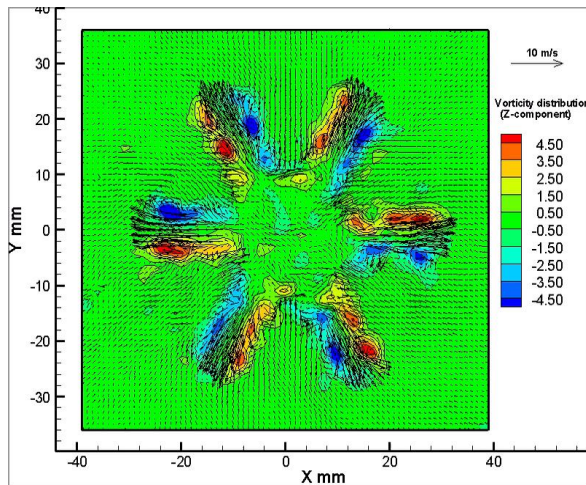


b. instantaneous vorticity  $\varpi_y$

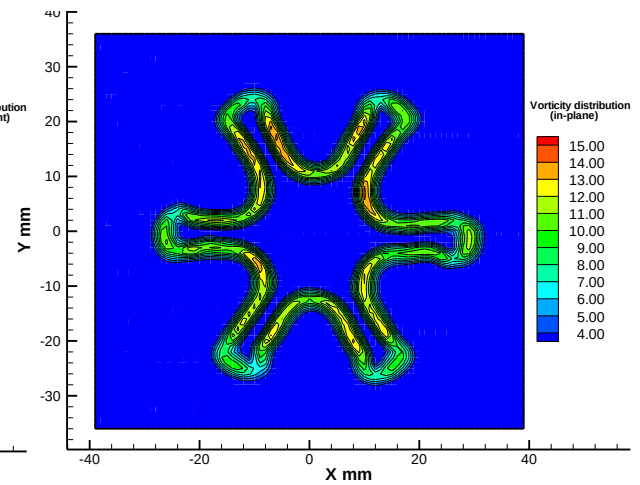


d. instantaneous azimuthal vorticity

$$\varpi_{in-plane} = \sqrt{\varpi_x^2 + \varpi_y^2}$$



e. ensemble-averaged streamwise vorticity  $\varpi_z$



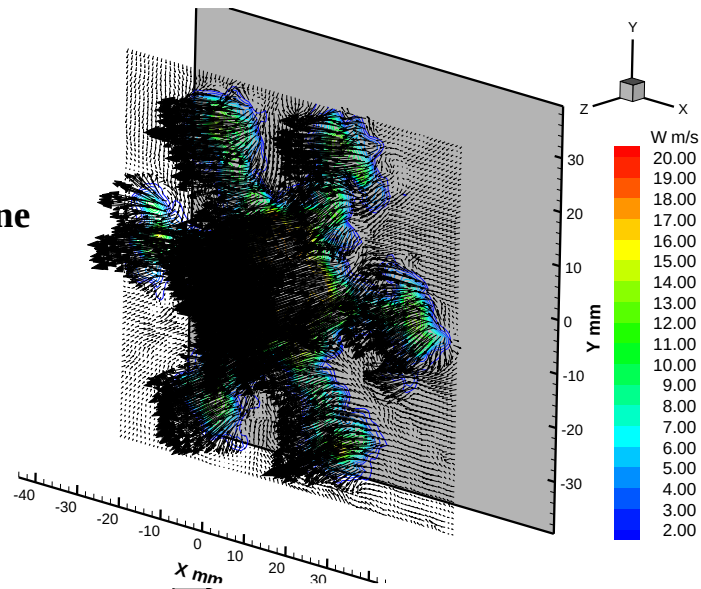
f. ensemble-averaged azimuthal

$$\text{vorticity } \varpi_{in-plane} = \sqrt{\varpi_x^2 + \varpi_y^2}$$

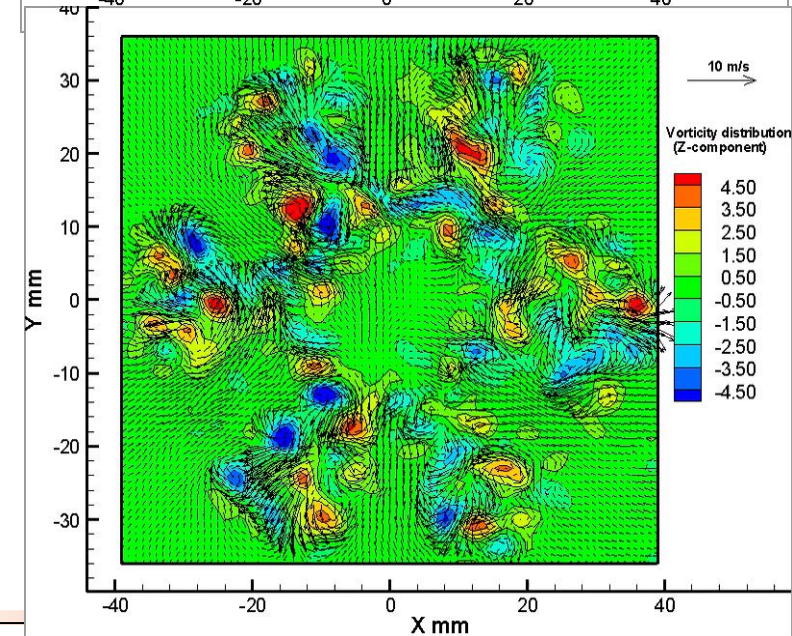
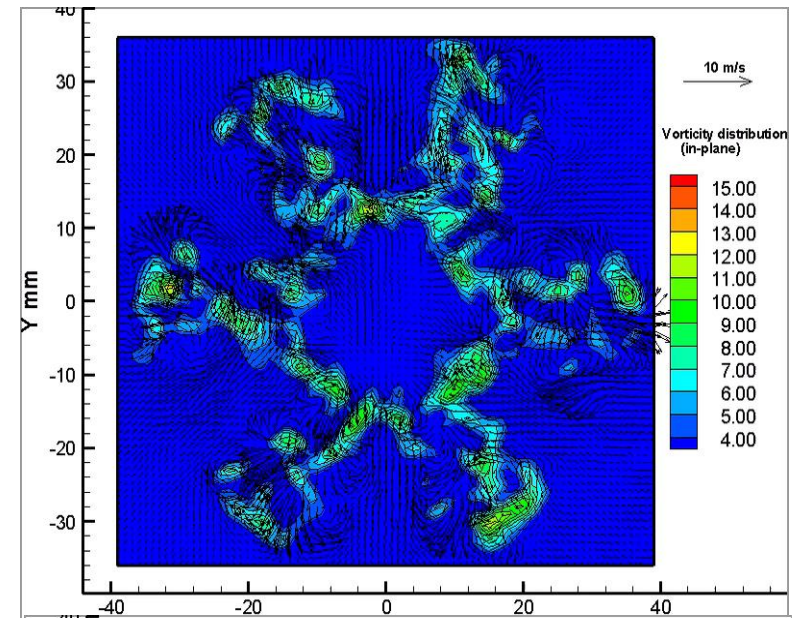
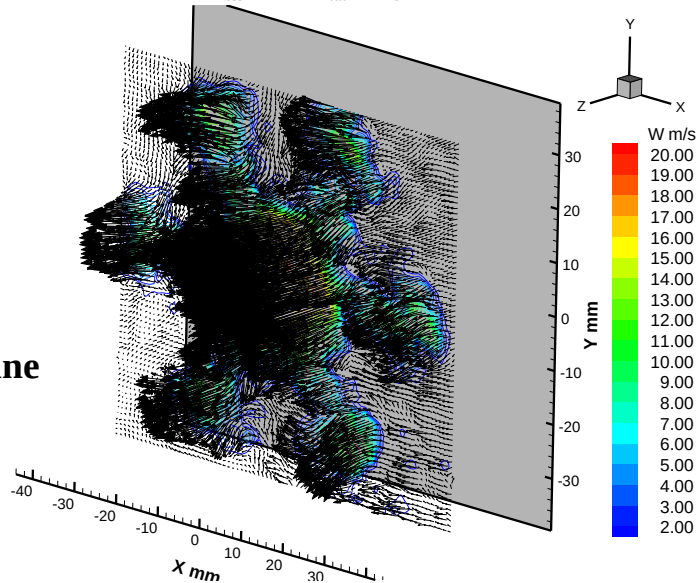
- [Hu H, Saga T, Kobayashi T, Taniguchi N, Yashuki M](#), "Dual-plane Stereoscopic Particle Image Velocimetry: System Setup and Its Application on a Lobed Jet Mixing Flow" *Experiments in Fluids*, Vol. 31, No. 3, pp277-293, 2001

# Measurement Results of the Dual-plane Stereoscopic PIV System

Z=40mm plane

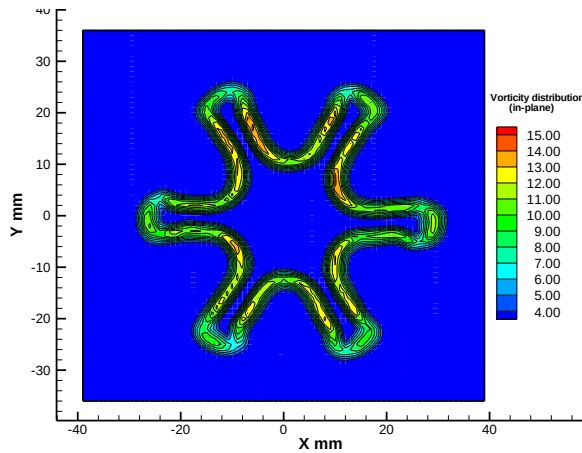


Z=42mm plane

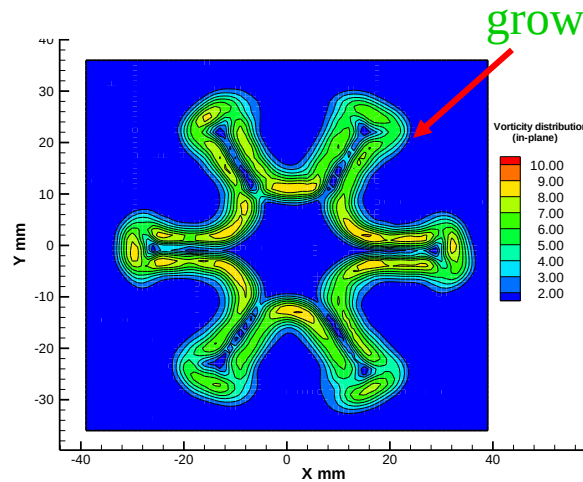




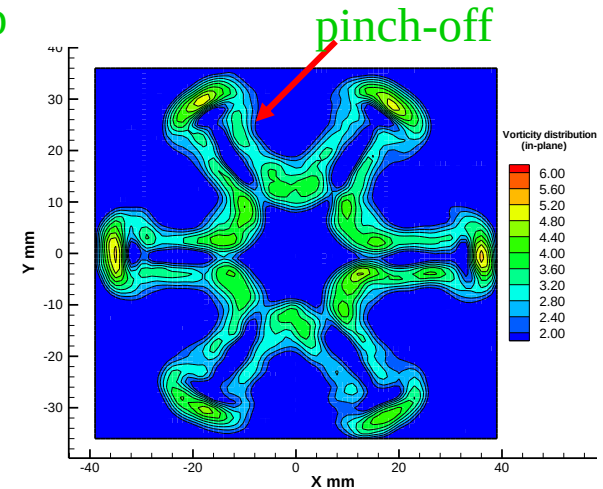
# Evolution of Spanwise Kelvin-Helmholtz Vortex Structures



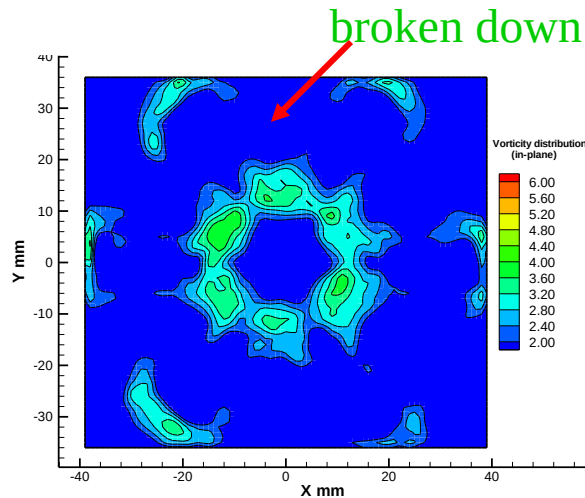
a. Z=10mm cross plane  
(Z/D=0.25)



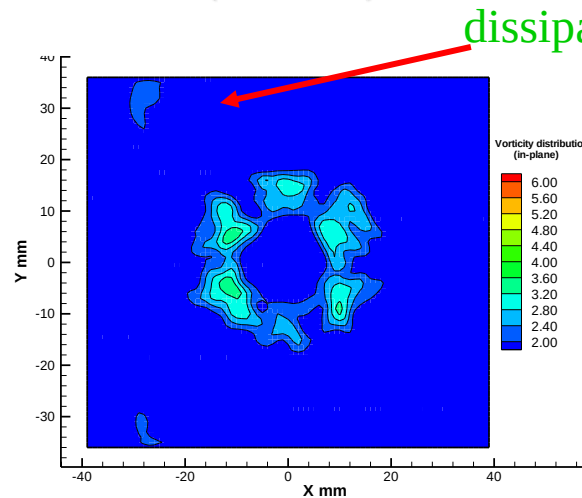
b. Z=20mm cross plane  
(Z/D=0.50)



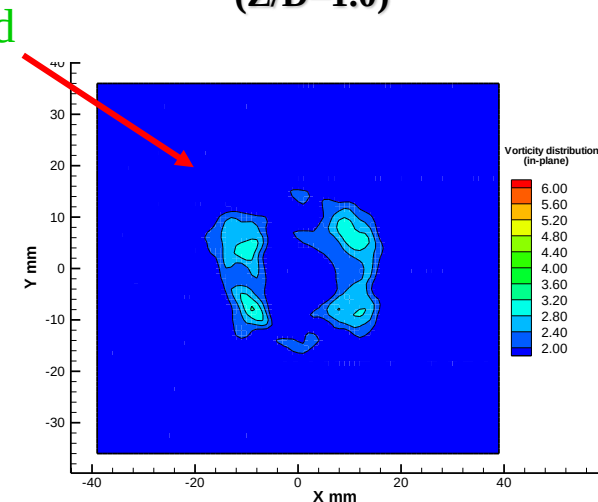
c. Z=40mm cross plane  
(Z/D=1.0)



d. Z=60mm cross plane  
(Z/D=1.5)

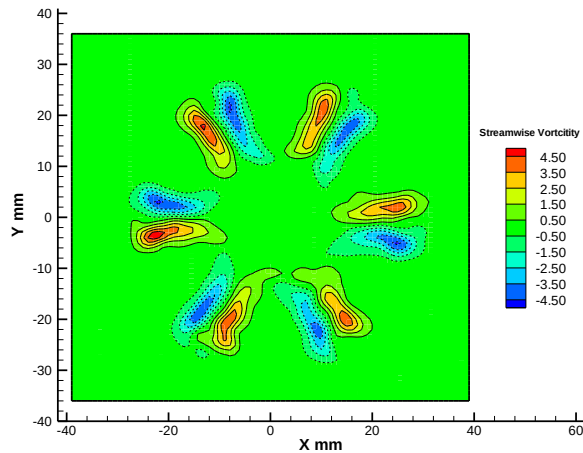


e. Z=80mm cross plane  
(Z/D=2.0)

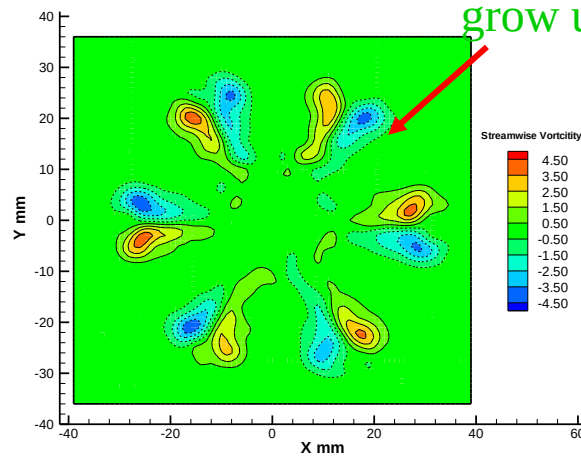


f. Z=120mm cross plane  
(Z/D=3.0)

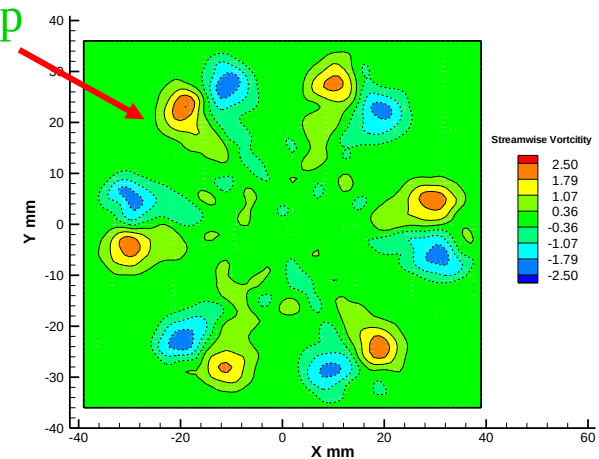
# Evolution of Large-scale Streamwise Vortex Structures



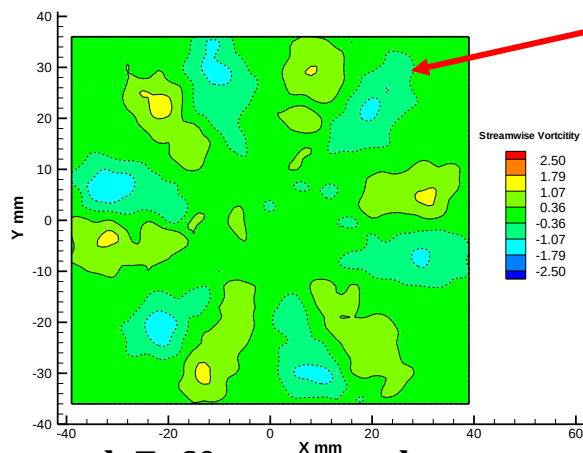
a. Z=10mm cross plane  
(Z/D=0.25)



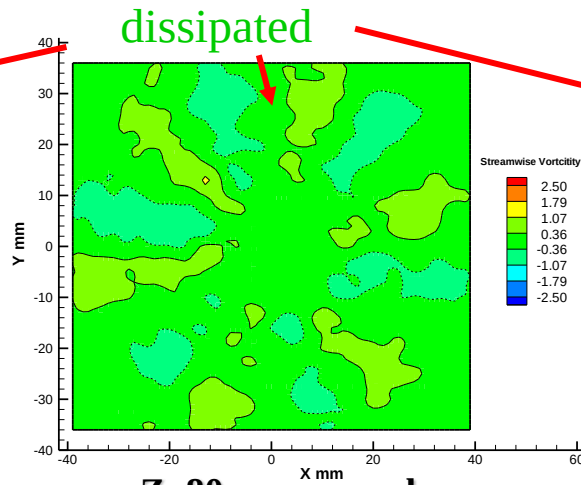
b. Z=20mm cross plane  
(Z/D=0.50)



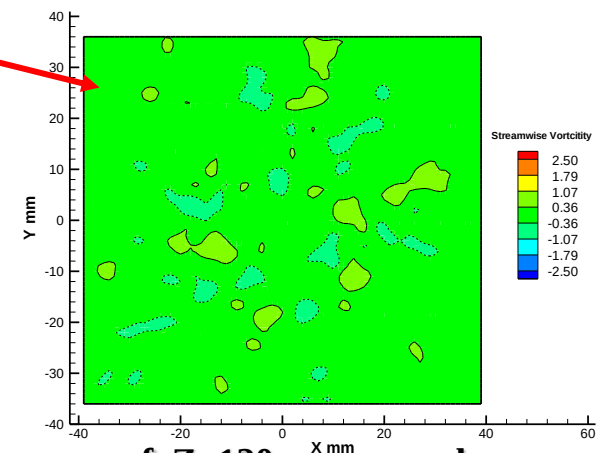
c. Z=40mm cross plane  
(Z/D=1.0)



d. Z=60mm cross plane  
(Z/D=1.5)



e. Z=80mm cross plane  
(Z/D=2.0)

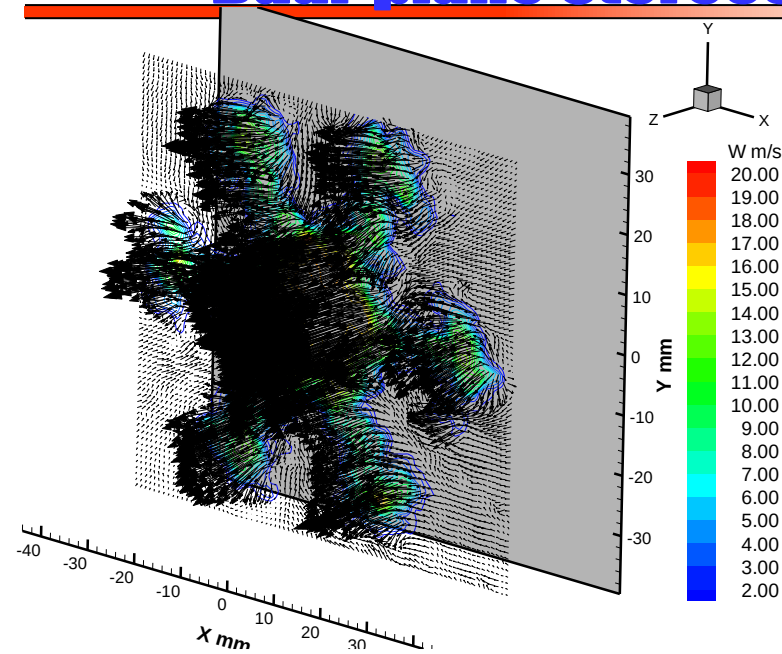


f. Z=120mm cross plane  
(Z/D=3.0)

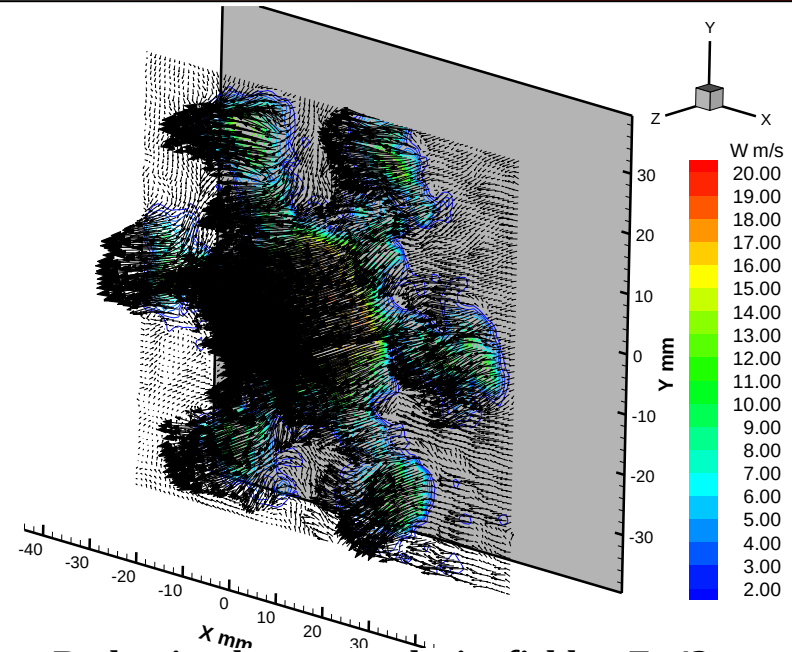
- [Hu H, Saga T, Kobayashi T, Taniguchi N, Yashuki M](#), "Dual-plane Stereoscopic Particle Image Velocimetry: System Setup and Its Application on a Lobed Jet Mixing Flow" *Experiments in Fluids*, Vol. 31, No. 3, pp277-293, 2001



# The Simultaneous Measurement Results of the Dual-plane Stereoscopic PIV at two separate planes



A. Instantaneous velocity field at Z=40mm plane



B. the simultaneous velocity field at Z=42mm plane

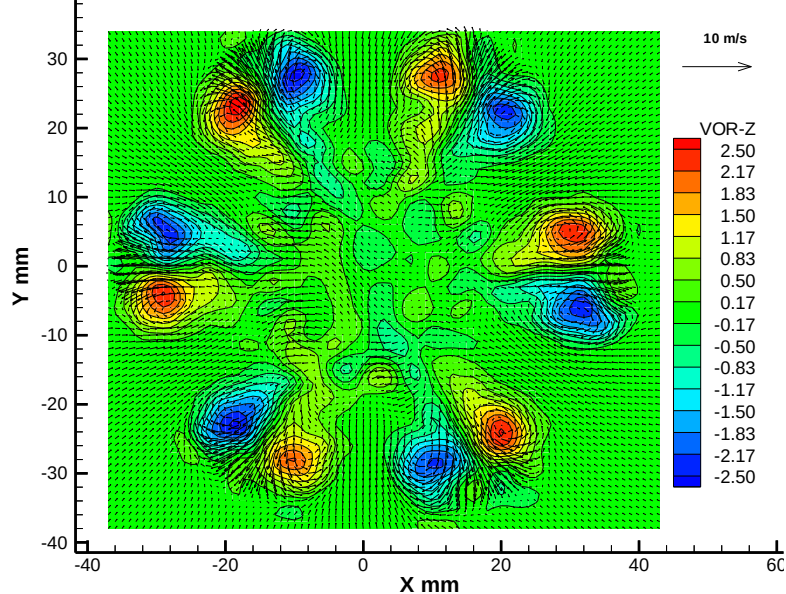
All three components of vorticity vectors:

$$\varpi_x = \frac{D}{U_0} \left( \frac{\partial w}{\partial y} - \frac{\partial v}{\partial z} \right); \varpi_y = \frac{D}{U_0} \left( \frac{\partial u}{\partial z} - \frac{\partial w}{\partial x} \right); \varpi_z = \frac{D}{U_0} \left( \frac{\partial v}{\partial x} - \frac{\partial u}{\partial y} \right)$$

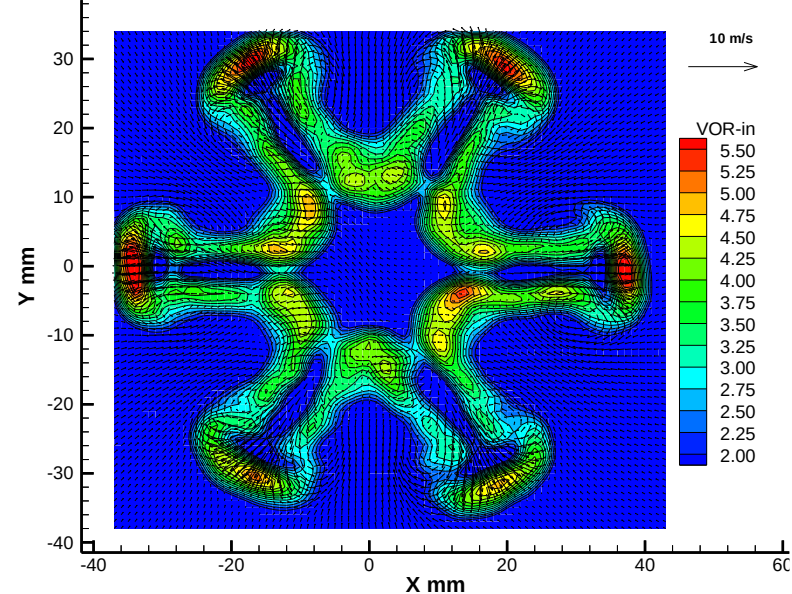
Cross correlation coefficient of flow variables at  $Z=Z_1$  and  $Z=Z_2$  planes:

$$\text{Cross} - R(u', v', w') = \frac{1}{N} \sum_{t=1}^{t=N} (u'(x, y, z_1, t) \bullet u'(x, y, z_2, t) + v'(x, y, z_1, t) \bullet v'(x, y, z_2, t) + w'(x, y, z_1, t) \bullet w'(x, y, z_2, t))$$

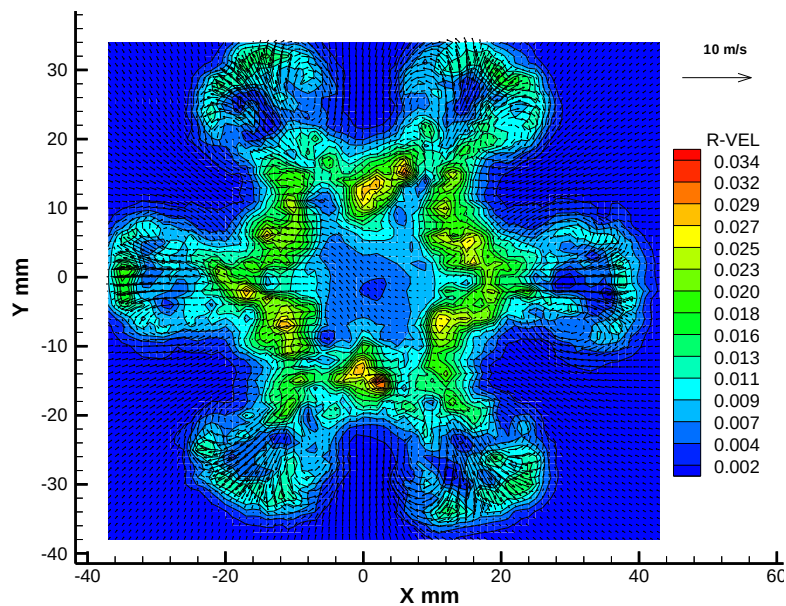
$$\text{Cross} - R(\varpi_z) = \frac{1}{N} \sum_{t=1}^{t=N} \varpi_z(x, y, z_1, t) \bullet \varpi_z(x, y, z_2, t)$$



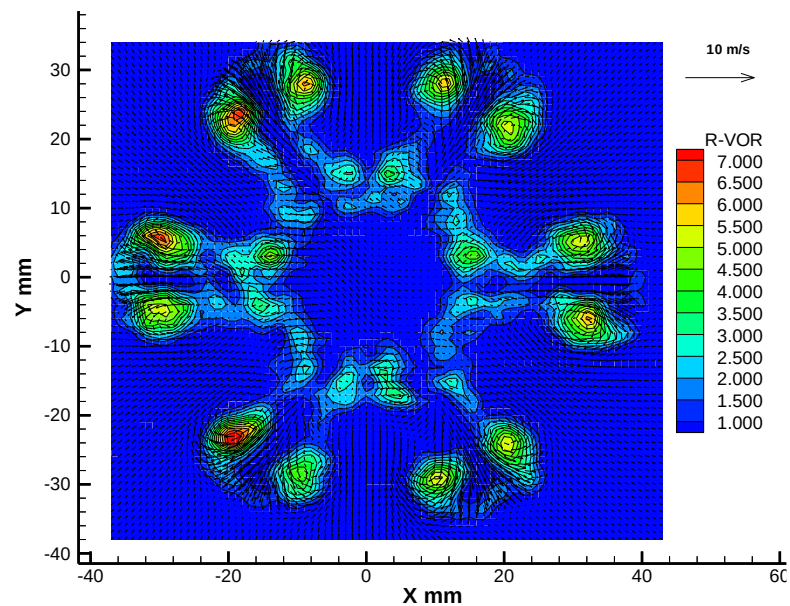
**A. ensemble averaged streamwise vorticity**



**B. ensemble averaged in-plane vorticity**



**C. cross-correlation coefficients of turbulent velocity**



**D. cross-correlation coefficients of streamwise vorticity**

***In the Z=40 mm cross plane of the lobed jet flow***

# The auto-correlation coefficients measurement with two illuminating laser sheets overlapped at the same plane

- *The temporal resolution of conventional PIV systems is limited to the framing rate of the cameras used for PIV image recording. Such limitation is much more serious for the PIV systems with high-resolution digital cameras. For example, the frame rate of a 1K by 1K pixel camera is always about 15Hz and much lower for the cameras with higher resolution. Therefore, a conventional PIV system is typically insufficient to record time sequences in rapidly evolving or turbulent flows. Therefore, only time-averaged quantities, such as the mean velocity and Reynolds stress, can be obtained to characterize the flow unsteadiness.*
- *The limitation of the slow framing rate of image recording camera can be over-passed by the present dual-plane stereoscopic PIV system. By adjusting the two illuminating laser sheets overlapped at the same plane, the flow field can be measured synchronously at variable separation times up to  $\mu$ s order.*

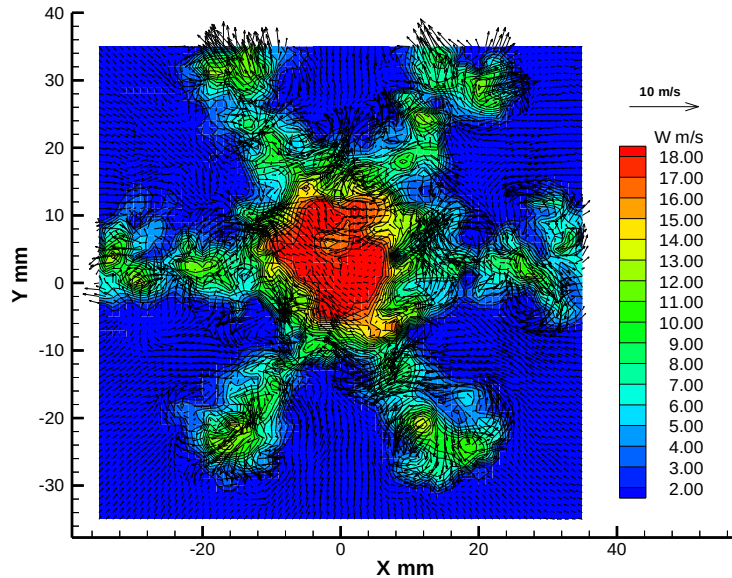
$$\text{Auto-R}(X) = \frac{1}{N} \sum_{n=0}^{N-1} X_n(x, y, z, t) \bullet X_n(x, y, z, t + \tau)$$

- [Hu H, Saga T, Kobayashi T, Taniguchi N, Yashuki M, "Dual-plane Stereoscopic Particle Image Velocimetry: System Setup and Its Application on a Lobed Jet Mixing Flow" Experiments in Fluids, Vol. 31, No. 3, pp277-293, 2001](#)

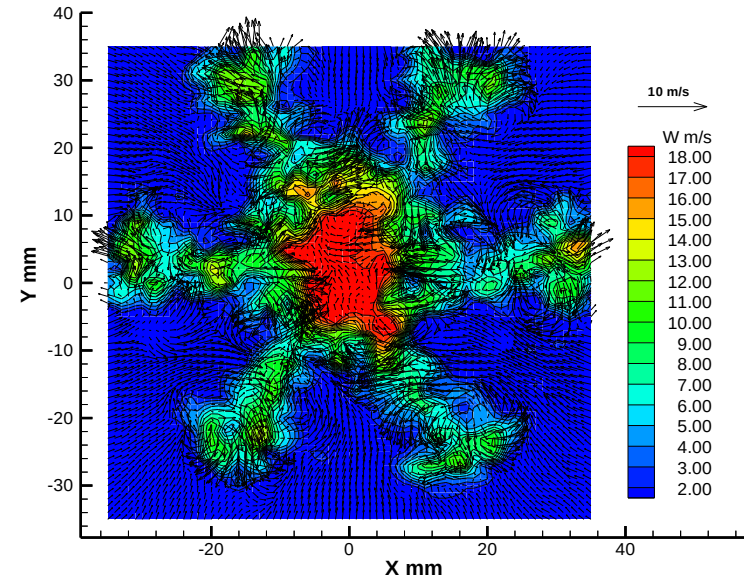


# The Measurement Results of the Dual-plane Stereoscopic PIV system

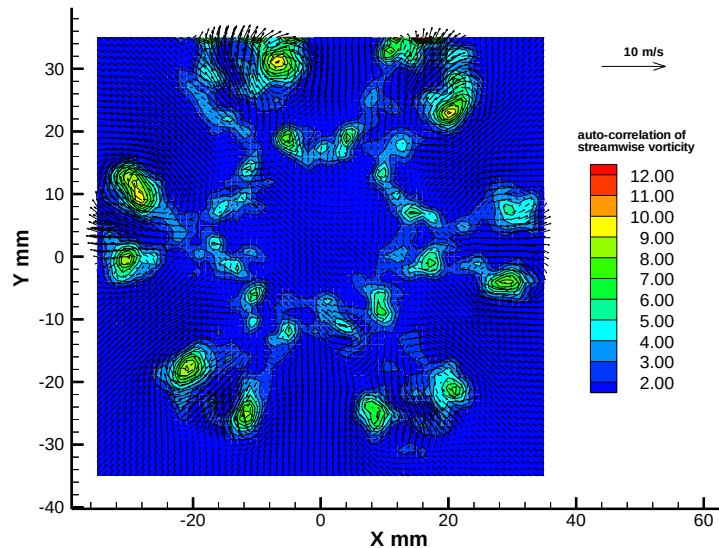
(the two illuminating laser sheets overlapped at the same  $Z=40\text{mm}$  plane with  $0.1\text{ms}$  time delay)



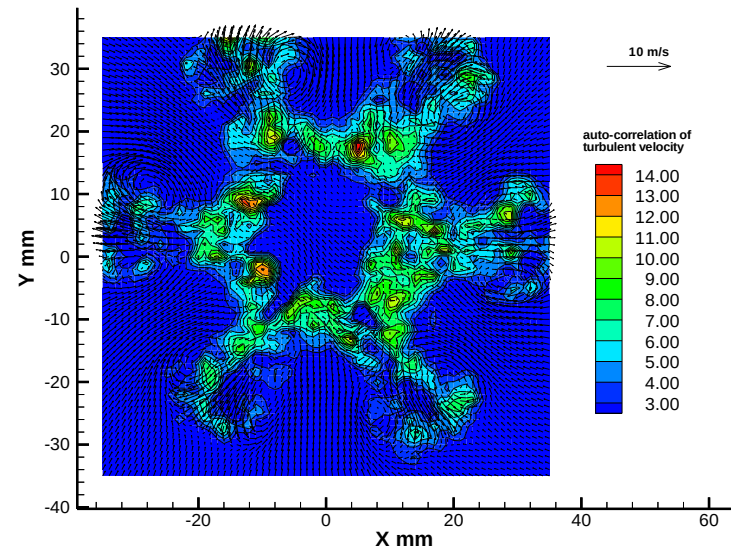
**A. instantaneous velocity field at time  $t=T_0$**



**B. instantaneous velocity field at time  $t=T_0+0.1\text{ms}$**



**C. auto-correlation of the streamwise vorticity**

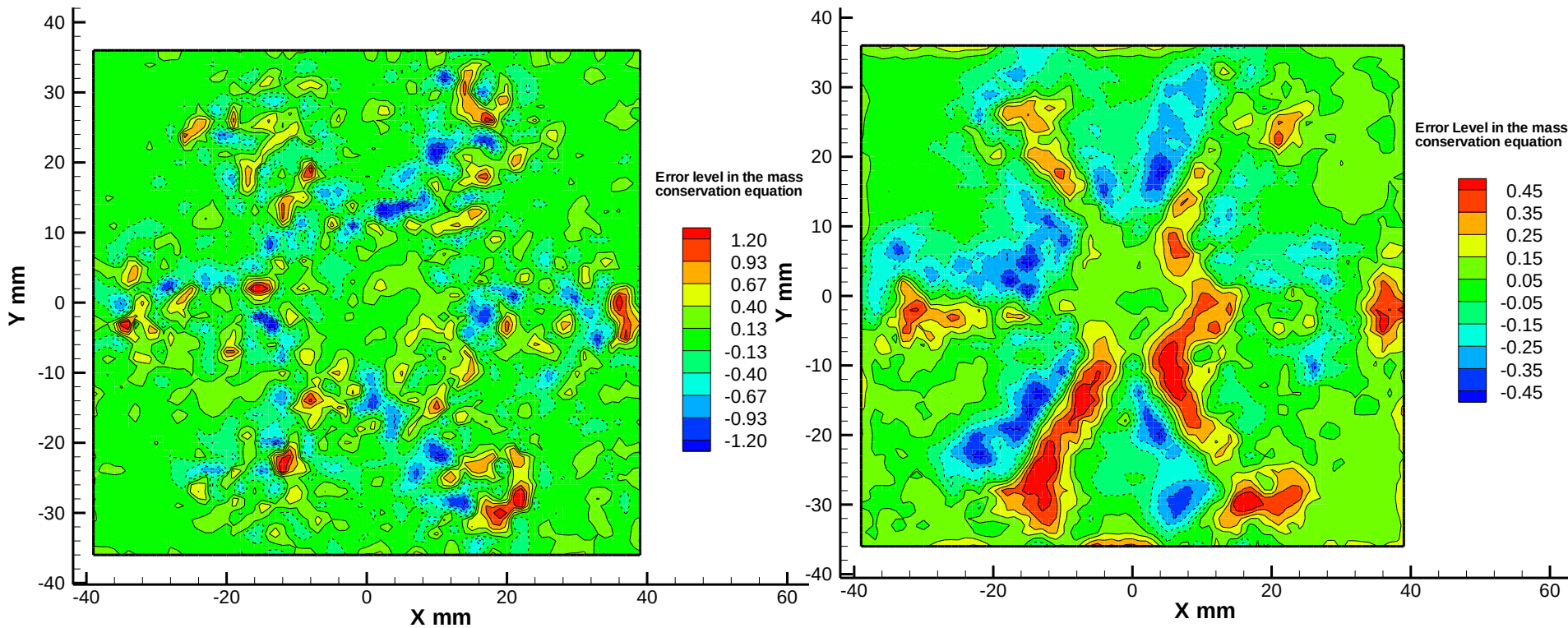


**D. auto-correlation coefficients of the turbulent velocity**

# Mass Conservation Equation

$$Q = \frac{D}{U_0} \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} + \frac{\partial w}{\partial z} \right)$$

*Z=40mm cross plane*



*Instantaneous distribution  
(averaged value  $Q=0.35$ )  
(equivalent error velocity  $\Delta w/U_0=1.75\%$ )*

*ensemble-averaged distribution  
(averaged value  $Q=0.13$ )  
(equivalent error velocity  $\Delta w/U_0=0.65\%$ )*